	Transforms	Slot	CI+1CI+TCC1
Time		Class Nbr	CH2024250500803
The state of the s	3 hours	Max. Marks	100
Instructio	ns To Candidates		
• Writ	e only your registration number	in the designated how and	
on th	e question paper will be consider	red a violation	question paper. Writing anything elsewhere

Course Outcomes

CO1: Find solution for second and higher order differential equations, formation and solving partial differential

CO2: Understand basic concepts of Laplace Transforms and solve problems with periodic functions, step functions, impulse functions and convolution.

CO3: Employ the tools of Fourier series and Fourier transforms.

CO4: Know the techniques of solving differential equations and partial differential equations.

CO5: Know the Z-transform and its application in population dynamics and digital signal processing.

Answer any 10 Questions (10×10 Marks)

01. Find the general solution of the differential equation $(D^2 - 2D + 1)y = 5e^{4x}$

[10] (CO1/K1

- 02. a. Find the charge q(t) on the capacitor in an LRC circuit when $L=0.25\,\mathrm{henry}(\mathrm{h})$ $R = 10 \text{ Ohm } (\Omega), \ C = 0.001 \text{ farad}(f)$ -, E(t) = 0, q(0) = 10 Coulombs(C), and i(0) = 0. (5 Marks) b. Form the PDE by eliminating arbitrary function f from the relation yz + zx + xy = f(z/(x+y)). (5 Marks)
- 03. Find the general solution of the partial differential equation $z(z^2 + xy)(px qy) = x^4$

[10] (CO1/K2)

[10] (CO1/K3)

04. (a) Express $f(t) = \begin{cases} 0, & 0 < t < \pi/2 \\ sin(t), & \pi/2 < t \end{cases}$, interms of heaviside function and find the Laplace transform of f(t)

b. Obtain Fourier series of the function $f(x) = \begin{cases} x, & -\pi < x < 0 \\ -x, & 0 < x < \pi \end{cases}$. (5 Marks)

[10] (CO2/K1)

05. Find
$$L^{-1}\left(\frac{(s+1)e^{-\pi s}}{s^2+s+1}\right)$$
.

[10] (CO2/K2)

06. Solve following initial value the problem (IVP) using Laplace the transform: $\frac{d^2x}{dt^2} - 2\frac{dx}{dt} + x = e^t$; x(0) = 2 and x'(0) = -1

[10] (CO4/K3) 07. By using the Laplace transform, solve the partial differential equation $\frac{\partial u}{\partial x} + 6x \frac{\partial u}{\partial t} = 12x$, with

u(0,t) = 2, for t > 0 and u(x,0) = 2, for x > 0. [10] (CO4/K3)

- Find the Fourier series of $f(x) = \begin{cases} 1 + \frac{2x}{\pi}, & -\pi < x < 0 \\ 1 \frac{2x}{\pi}, & 0 < x < \pi \end{cases}$. Hence deduce that $\frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$ [10] (CO3/K2)
- 09. Find the Fourier transform of the given Gaussian function $f(x) = 2e^{-3x^2}$.

[10] (CO3/K1)

- 10. Find the Fourier transform of $f(x) = \frac{e^{-ax}}{x}$ and use it to evaluate $\int_0^\infty \tan^{-1}\left(\frac{x}{a}\right) \sin\left(x\right) dx$.
- [10] (CO3/K5)

11. If $u_n = \sin^2(3n+5) + (n-1)^3$, then find the Z-Transform of u_n

[10] (CO5/K5)

12. Solve $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$ with $y_0 = 1 & y_1 = 0$ by using Z-Transform.

[10] (CO5/K3)

BL-Bloom's Taxonomy Levels - (K1-Remembering, K2-Understanding, K3-Applying, K4-Analysing, K5-Evaluating, K6-Creating)

